PULSARS AND PULSAR WIND NEBULAE Lecture 2

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OUTLINE OF LECTURE 2

- SUMMARY OF LECTURE 1
- MHD MODELING OF NEBULAE AND THEIR RADIATION
 - 1-D MHD MODELING
 - 2-D MHD MODELING
 - VARIABILITY
- PARTICLE ACCELERATION AT THE MOST RELATIVISTIC SHOCKS IN NATURE
- OLD NEBULAE, FAST PULSARS AND THE ELECTRON-POSITRON EXCESS IN COSMIC RAYS

SUMMARY OF LECTURE 1

PULSARS CANNOT BE SURROUNDED BY VACUUM •A COROTATING MAGNETOSPHERE DEVELOPS •COROTATION CANNOT EXTEND BEYON R_{LC} •NOT ALL FIELD LINES CAN BE CLOSED •PARTICLES LEAVE THE STAR ALONG OPEN FIELD LINES

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THE SYSTEM TRIES TO ACHIEVE E_{//}=0 EVERYWHERE BUT THIS IS NOT POSSIBLE WITH ONLY CHARGES FROM STAR SURFACE

THE WIND ZONE $J_{GJ} = c\rho_{GJ} = \frac{\vec{\Omega} \cdot \vec{B}}{2\pi}$ acts as source

 B_T COMPARABLE TO B_P AT THE LIGHT CYLINDER

IN VACUUM

AT LARGER DISTANCES FIELD LINES ARE OPEN: B_P MONOPOLE LIKE

$B_{p} = B_{r} = B_{LC} \left(\frac{R_{LC}}{r}\right)^{2} \text{ TOROID}$ BECON $B_{\phi} = \pm B_{LC} \left(\frac{R_{LC}}{r}\right) \sin \theta \text{ DOM}$	AL FIELD OMES INANT
$\dot{E} = \frac{c}{4\pi} 4\pi R_{LC}^2 \left(\vec{E} \times \vec{B}\right)_{R_{LC}} = c\dot{R}$	$R_{LC}^2 B_{LC}^2$
$\dot{E} = cB_*^2 R_*^2 \left(\frac{R_*^4 \Omega^4}{4} \right) $ ~SAME /	AS FOR DIPOLE

QuickTime[™] and a decompressor are needed to see this picture.

PULSAR SPIN DOWN

FOR ARBITRARY INCLINATION α BETWEEN **B** AND Ω

$$\dot{E} = cB_*^2 R_*^2 \left(\frac{R_*\Omega}{c}\right)^4 \left(1 + \sin^2\alpha\right)$$

$$\dot{E} = I\Omega\dot{\Omega} = -a\Omega^4$$

MORE GENERALLY: $\Omega = -a\Omega^n$ $E = I\Omega\Omega = aI\Omega^{n+1}$

AFTER INTEGRATION
$$\Omega(t) = \frac{\Omega_0}{\left[1 + t/\tau_0\right]^{1/(n-1)}} \qquad \tau_0 = \frac{\Omega_0^{1-n}}{a(n-1)}$$

 $\stackrel{\cdot}{\longrightarrow} \stackrel{\cdot}{E} = \frac{aI\Omega_0^{n+1}}{\left[1 + t/\tau_0\right]^{n+1}}$ n=BRAKING INDEX. n=3 FOR A DIPOLE FIELD AND <3 FOR OTHER CASES

DERIVING n IMPLIES MEASURING d²P/dt² MEASURED FOR 4 PSRs ONLY: ALWAYS LESS THAN 3!!!!

AVAILABLE POTENTIAL



UNSCREENED POTENTIAL ⇒ ACCELERATION TO E»"KNEE"

•WHERE THERE IS UNSCREENED E_{//} PARTICLES ARE QUICKLY ACCELERATED TO RELATIVISTIC ENERGIES •A PAIR CASCADE IS INITIATED



•CASCADES OVERSHOOT η_{GJ}.
 •BY HOW MUCH DEPENDS ON MODEL.
 •MULTIPLICITY?

PAIR PRODUCTION SITES

POLAR CAPS

OUTER GAPS



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SLOT GAPS



PAIR PRODUCTION AND



 γ -RAY EMISSION **•USE γ-RAYS TO LEARN ABOUT** PAIR PRODUCTION **•POLAR CAPS MODELS, THE ONES** WITH CLEAREST PREDICTIONS **ON MULTIPLICITY, EXCLUDED** AS MAIN SOURCE OF γ -RAYS SLOT GAPS AND OUTER GAPS **ARE HEAVILY CHALLENGED BY NEW OBSERVATIONS AND FORCE-FREE SIMULATIONS** FORCE-FREE IS BETTER APPROX THAN VACUUM

FOLLOW THE ENERGY

MOST PULSAR ENERGY GOES INTO PWN



$$\dot{E}_{R} = \frac{B_{0}^{2} R_{0}^{6} \Omega^{4}}{c^{3}} = \int d\vec{S} \left[\frac{c}{4\pi} \vec{E} \times \vec{B} + \Gamma_{wind} \left(n_{\pm} m_{e} + n_{i} m_{i} \right) c^{3} \right]$$

$$\overset{\bullet}{E}_{R} = \kappa \overset{\bullet}{N}_{GJ} m_{\pm} c^{2} \Gamma_{wind} \left(1 + \frac{m_{i}}{\kappa m_{\pm}} \right) (1 + \sigma)$$

WE MEASURE IT

•

$$N_{GJ} \approx \pi R_0^2 \,\mathcal{P}_p^2 c \left| \frac{\eta_{GJ0}}{e} \right| \approx 3 \times 10^{32} \frac{\mu_{30}}{P_{100}^2} \, s^{-1}$$

DEPENDS ONLY ON MEASURED PSR PARAMETERS



CAN BE EVALUATED FROM PWN SYNC. EMISSION KNOWING B

$$\sigma = \frac{B^2}{4 \,\pi \, m_{eff} n_{eff} c^2 \, \Gamma_{wind}^2}$$

MUST BE LARGE AT LC: σ≈10⁴-10⁶ PROBABLY SMALL IN THE PWN BASED ON MHD MODELING

MAGNETIC FIELD IN NON-THERMAL SOURCES

•EQUIPARTITION •SYNCHROTRON AGE BREAK •RATIO BETWEEN ICS AND SYNCHROTRON EMISSION





1-ZONE MODELS FOR THE PWN EVOLUTION

CHANGING PULSAR INPUT EVOLUTION OF PARTICLES AND MAGNETIC FIELD



Bucciantini, Arons, Amato 2012

HOW TO MAKE PROGRESS

•1-ZONE MODELS SUGGEST HIGH MULTIPLICITIES
•THEY CANNOT BE CONSIDERED CONCLUSIVE:
ASSUMPTIONS ON WIND EVOLUTION MIGHT BE FLAWED
•THEY ONLY PROVIDE INFO ON AVERAGE QUANTITIES
•THEY DO NOT REALLY PROVIDE INFO ON σ

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DETAILED MHD MODELING WHEN POSSIBLE

MHD MODELS OF PWNe: ASSUMPTIONS

1-D STEADY-STATE HD (Rees & Gunn 74)
1-D STEADY-STATE MHD (Kennel & Coroniti 84)
1-D SELF-SIMILAR MHD (Emmering & Chevalier 87)
2-D STATIC MHD (Begelman & Li 92)

RN Synchrotron bubble

GENERAL ASSUMPTIONS

COLD ISOTROPIC MHD WIND
STRONG PERP. REL. SHOCK
SUBSONIC FLOW IN THE NEBULA
PARTICLE ACCELERATION AT THE TS
SYNCHROTRON LOSSES THEREAFTER

MAIN FREE PARAMETERS •WIND MAGNETIZATION $\sigma = \frac{B^2}{4\pi nmc^2\Gamma^2}$ •LORENTZ FACTOR Γ •PARTICLE SPECTRAL INDEX α

THE KENNEL AND CORONITI MODEL

(Kennel & Coroniti, 1984a, 1984b)

0

FREE PARAMETERS

WIND MAGNETIZATION

σ= B²/(4πnmc²Γ²)

LORENTZ FACTOR Γ

SPECTRAL INDEX α

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> QuickTime™ and a YUV420 codec decompressor are needed to see this picture.

RELATIVISTIC MHD EQUATIONS IN SPHERICAL SYMMETRY

∂	- 0
$\overline{\partial} t$	$t^{-} = 0$

$$\frac{1}{r^2} \frac{\partial}{\partial r} (r^2 n u) = 0$$

$$\frac{1}{r} \frac{\partial}{\partial r} (\frac{r u B}{\gamma}) = 0$$

$$\frac{1}{r^2}\frac{\partial}{\partial r}\left[r^2\left(w\,u^2+p+\frac{B^2}{8\pi}\left(1+\frac{u^2}{\gamma^2}\right)\right)\right]-\frac{2p}{r}=0$$

$$\frac{1}{r^2} \frac{\partial}{\partial r} \left[r^2 \left(w \, \gamma \, u + \frac{B^2}{4 \, \pi} \frac{u}{\gamma} \right) \right] = 0$$

ENERGY CONSERVATION

SHOCK IS ASSUMED STEADY STATE INTEGRATE EQUATIONS ACROSS THE SHOCK: $\Delta x \rightarrow 0$

$$n_{1}u_{1} = n_{2}u_{2} \qquad \qquad \frac{u_{1}B_{1}}{\gamma_{1}} = \frac{u_{2}B_{2}}{\gamma_{2}}$$

$$\mu_{1}n_{1}u_{1}^{2} + p_{1} + \frac{B_{1}^{2}}{8\pi} \left(1 + \frac{u_{1}^{2}}{\gamma_{1}^{2}}\right) = \mu_{2}n_{2}u_{2}^{2} + p_{2} + \frac{B_{2}^{2}}{8\pi} \left(1 + \frac{u_{2}^{2}}{\gamma_{2}^{2}}\right)$$

$$B_{1}^{2}u_{1} \qquad \qquad B_{2}^{2}u_{2}$$

 $\mu_1 n_1 u_1 \gamma_1 + \frac{1}{4\pi} \frac{1}{\gamma_1} = \mu_2 n_2 u_2 \gamma_2 + \frac{1}{4\pi} \frac{1}{\gamma_2}$

$$\mu = \frac{w}{n}$$

THE SHOCK JUMP

(

ASSUMPTIONS: •HIGHLY RELATIVISTIC SHOCK •UPSTREAM FLUID IS COLD

$$\gamma_1 >> 1 \Longrightarrow u_1 \approx \gamma_1$$
$$\frac{p_1}{n_1 m c^2} \to 0, \quad \mu_1 \to m c^2$$

$$\sigma = \frac{B_1^2}{4\pi n_1 u_1 \gamma_1 mc^2}$$

$$u_{2}^{2} = \frac{1}{2} \left\{ \frac{8\sigma^{2} + 10\sigma + 1}{8(1 + \sigma)} \pm \sqrt{\left(\frac{8\sigma^{2} + 10\sigma + 1}{8(1 + \sigma)}\right)^{2} - \frac{\sigma^{2}}{2(1 + \sigma)}} \right\}$$

IMPOSING POSITIVE DOWNSTREAM PRESSURE ALLOWS TO SELECT CORRECT SOLUTION

$$u_{2}^{2} = \frac{1}{2} \left\{ \frac{8\sigma^{2} + 10\sigma + 1}{8(1 + \sigma)} \pm \sqrt{\left(\frac{8\sigma^{2} + 10\sigma + 1}{8(1 + \sigma)}\right)^{2} - \frac{\sigma^{2}}{2(1 + \sigma)}} \right\} \qquad \gamma_{2} = \sqrt{1 + u_{2}^{2}}$$
$$\frac{p_{2}}{n_{1}mc^{2}\gamma_{1}^{2}} = \frac{1}{4u_{2}\gamma_{2}} \left[1 + \sigma \left(1 - \frac{\gamma_{2}}{u_{2}}\right) - \frac{\gamma_{2}}{\gamma_{1}} \right] \qquad \frac{B_{2}}{B_{1}} = \frac{\gamma_{2}}{u_{2}}$$

LARGE AND SMALL σ

$$u_{2}^{2} = \frac{1}{2} \left\{ \frac{8\sigma^{2} + 10\sigma + 1}{8(1 + \sigma)} \pm \sqrt{\left(\frac{8\sigma^{2} + 10\sigma + 1}{8(1 + \sigma)}\right)^{2} - \frac{\sigma^{2}}{2(1 + \sigma)}} \right\} \qquad \gamma_{2} = \sqrt{1 + u_{2}^{2}}$$
$$\frac{p_{2}}{n_{1}mc^{2}\gamma_{1}^{2}} = \frac{1}{4u_{2}\gamma_{2}} \left[1 + \sigma \left(1 - \frac{\gamma_{2}}{u_{2}}\right) - \frac{\gamma_{2}}{\gamma_{1}} \right] \qquad \frac{B_{2}}{B_{1}} = \frac{\gamma_{2}}{u_{2}}$$

IF B-FIELD DOMINATES DYNAMICS:



•FLUID DOES NOT SLOW
DOWN AT SHOCK
•PRESSURE STAYS LOW
(LITTLE DISSIPATION)
•B-FIELD FURTHER
INCREASES EVEN IF LITTLE

$$\sigma \to 0$$

$$u_2^2 \to \frac{1+9\sigma}{8}$$

$$\gamma_2^2 \to \frac{9}{8}(1+\sigma)$$

$$\frac{p_2}{n_1 m c^2 \gamma_1^2} \to \frac{2}{3}(1-7\sigma)$$

$$\frac{B_2}{B_1} = \frac{N_2}{N_1} \to 3-12\sigma$$

IN FIGURES....



IDENTIFY and Set UP:
(1)
$$\frac{1}{r^2} \frac{\partial}{\partial r} (r^2 n u) = 0$$
 (3) $\frac{1}{r^2} \frac{\partial}{\partial r} \left[r^2 \left(w u^2 + p + \frac{B^2}{8\pi} \left(1 + \frac{u^2}{\gamma^2} \right) \right) \right] - \frac{2p}{r} = 0$
(2) $\frac{1}{r} \frac{\partial}{\partial r} \left(\frac{r u B}{\gamma} \right) = 0$ (4) $\frac{1}{r^2} \frac{\partial}{\partial r} \left[r^2 \left(w \gamma u + \frac{B^2}{4\pi} \frac{u}{\gamma} \right) \right] = 0$

$$\frac{\partial}{\partial r} \left(\frac{p}{n^{\Gamma}} \right) = 0$$

$$\left(\mu\gamma + \frac{B^2}{4\pi n\gamma}\right) = \cos t$$

$$\mu = mc^2 + \frac{\Gamma}{\Gamma - 1} \frac{p}{n}$$

$$nur^{2} = n_{2}u_{2}r_{s}^{2} \qquad \qquad \frac{uBr}{\gamma} = \frac{u_{2}B_{2}r_{s}}{\gamma_{2}}$$
$$\frac{p}{n^{\Gamma}} = \frac{p_{2}}{n_{2}^{\Gamma}} \qquad \qquad \gamma \left(mc^{2} + \frac{\Gamma}{\Gamma - 1}\frac{p}{n} + \frac{B^{2}}{4\pi n\gamma^{2}}\right) = \gamma_{2}\left(mc^{2} + \frac{\Gamma}{\Gamma - 1}\frac{p_{2}}{n_{2}} + \frac{B_{2}^{2}}{4\pi n_{2}\gamma_{2}^{2}}\right)$$



FOR LARGE σ TERMINAL VELOCITY STAYS RELATIVISTIC IN CRAB v_N=1000km/s e $\sigma=v_N/c=0.003$

MAGNETIC FIELD



SPECTRAL EVOLUTION

INJECTION SPECTRUM AT SHOCK: $f_2(E_2) = KE_2^{-p}$

CONSERVATION OF PARTICLE NUMBER

 $4\pi r^2 cuf(E,z)dE = 4\pi r_s^2 cf_2(E_2)dE_2 \quad \Rightarrow \quad f(E,z) = \frac{1}{\sqrt{z^2}} f_2[E_2(E,z)]\frac{\partial E_2}{\partial E}$

$E_2(E,z) = ?$



(p-2) $f(E,z) = \frac{KE^{-p}}{(vz^2)^{(2+p)/3}} \left[1 - \frac{E}{E_{\infty}(z)} \right]^{(vz)}$

 $E_{\infty}(z)$ MAXIMUM PARTICLE ENERGY AT ANY PLACE

NEBULAR SIZE

CRITICAL FREQUENCY

FORM FACTORS

$$v_{\infty}(z) = \frac{3}{4\pi} \left(\frac{eB_2}{mc}\right) \frac{1}{vz} \left(\frac{E_{\infty}(z)}{mc^2}\right)^2$$

$$I_{\nu}(z_{\perp}) = 2 \int_{z_{\perp}}^{z_{\mu}} dz \frac{J_{\nu}(z)z}{\sqrt{\left(z^2 - z_{\perp}^2\right)}}$$

NEBULAR SIZE DECREASES WITH INCREASING OBS. FREQUENCY

QuickTime™ and a decompressor are needed to see this picture.

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INTEGRATED SPECTRUM

INTEGRATED SPECTRUM SHOWS STEEPENING DUE TO DECREASING NEBULAR VLUME WITH INCREASING FREQUENCY

QuickTime™ and a decompressor are needed to see this picture.

MHD MODELS OF PWNe: PREDICTIONS



INTEGRATED EMISSION SPECTRUM FROM OPTICAL TO X-RAYS AND EVEN γ-RAYS (de Jager & Harding 92; Atoyan & Aharonian 96) **NO EXPLANATION FOR RADIO ELECTRONS**: MAYBE PRIMORDIAL (Atoyan 99)...

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ELONGATION



BASIC PARAMETERS AND QUESTIONS LEFT OPEN

 $R_{TS} \sim R_N (V_N/c)^{1/2} \sim 10^9 - 10^{10} R_{LC}$ FROM PRESSURE BALANCE (e.g. Rees & Gunn 74)

In Crab R_{TS} ~0.1 pc:

~boundary of underluminous (*cold wind*) region ~"wisps" location (variability over months) QuickTime™ and a YUV420 codec decompressor are needed to see this picture.



THEN CAME CHANDRA!





5.09 (Chande B1509-58 (X-rays+radio) (Slan: et al., 2009)







THE PUZZLING JET IN CRAB

JET IN CRAB APPEARED TO ORIGINATE FROM CLOSER TO THE PSR THAN $\rm R_{TS}$



MAGNETIC COLLIMATION IN RELATIVISTIC FLOW NOT AN OPTION (e.g. Lyubarsky & Eichler 01) $\Gamma \gg 1 \Rightarrow \rho \vec{E} + \vec{j} \times \vec{B} \approx 0$

COLLIMATION MUST OCCUR INSIDE THE NEBULA

(Bogovalov & Khangoulian 02; Lyubarsky 02)

ANISOTROPIC ENERGY FLUX OF THE WIND $F \propto sin^2(\theta)$ LEADS TO OBLATE TS, CLOSER TO THE PSR AT THE POLES THAN AT THE EQUATOR

THIS IS EXACTLY WHAT WIND MODELS PREDICT!

ANISOTROPIC WIND ENERGY FLOW

DENSE PLASMA WE SAID....



ANALYTIC SPLIT MONOPOLE SOLUTIONS (Michel 73; Bogovalov 99) CONFIRMED BY NUMERICAL STUDIES IN THE FORCE FREE (Contopoulos et al 99, Gruzinov 04, Spitkovsky 06) AND RMHD REGIME (Bogovalov 01, Komissarov 06, Bucciantini et al 06)

STREAMLINES BECOME ASYMPTOTICALLY RADIAL BEYOND RIC MOST ENERGY FLOWS AT LOW LATITUDES: $F\propto sin^2(\theta)$ MAGNETIC FIELD COMPONENTS: $B_{\phi} \propto \sin(\theta)/r$ $B_r \propto 1/r^2$ WITHIN IDEAL MHD σ STAYS LARGE **CURRENT SHEET IN EQUATORIAL PLANE: OSCILLATING AROUND EQUATOR IN OBLIQUE CASE** ANGULAR EXTENT DEPENDS ON OBLIQUITY

THE WIND MAGNETIZATION



RECENT STUDIES:

RECONNECTION NOT FAST ENOUGH AT MINIMUM RATE (Lyubarsky & Kirk 01)

•dN/dt~10⁴⁰ s⁻¹ REQUIRED FOR CRAB (Kirk & Skjaeraasen 03)

•THIS CONTRASTS WITH PSR THEORY (e.g. Hibschman & Arons 01: κ ~10³-10⁴ \Rightarrow dN/dt~10³⁸ for Crab) BUT JUST RIGHT FOR RADIO EMITTING PARTICLES

IN 2-D MHD SIMULATIONS $B \propto sin(\theta) G(\theta)$ with $G(\theta)$ accounting for decreasing magnetization toward equator

TERMINATION SHOCK STRUCTURE

AXISYMMETRIC RMHD SIMULATIONS OF PWNE

Komissarov & Lyubarsky 03, 04 Del Zanna et al 04, 06 Bogovalov et al 05







σ>0.01 REQUIRED FOR JET FORMATION

BEST FIT: FACTOR 10 LARGER THAN WITHIN 1D MHD MODELS

(Del Zanna et al 04)







SYNCHROTRON EMISSION MAPS





run B: surface brightness I, (X-ray)

E_{max} IS EVOLVED WITH THE FLOW f(E)∝E^{-α}, E<E_{max} (Del Zanna et al 06)

BETWEEN 3 AND 15 % OF THE WIND ENERGY FLOWS WITH σ<0.001







(Weisskopf et al 00)

(Pavlov et al 01)

THE CRAB NEBULA INTEGRATED EMISSION SPECTRUM

Quantitative fit of the spectral properties of the Crab Nebula requires injection spectrum with α =2.7!!!! But....



•Optical spectral index maps (Veron-Cetty & Woltjer 92) suggest flatter injection spectrum: $\alpha \sim 2.2$ (but see also Kargaltsev & Pavlov 09)

Suspicion that particles are loosing too little: average B too low?

In order to recover total flux number of particles artificially large

•Synchrotron only offers combined information on n_e and B: $L_{syn} \propto n_e B^2$

But computation of ICS offers additional constraints: $L_{ICS} \propto n_e U_{ph}$

γ-RAY SPECTRUM FROM CRAB



γ-RAY EMISSION FROM CRAB



γ-RAY VARIABILITY DUE TO MHD EFFECTS (the movie)



γ-RAY VARIABILITY DUE TO MHD EFFECTS



NO VARIATION (~1%) EXPECTED AT TEV ENERGIES

X-RAY VARIABILITY IN THE INNER NEBULA

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VARIABLE SHOCK STRUCTURE AND THE WISPS

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QuickTime[™] and a decompressor are needed to see this picture.

Camus, Komissarov, Bucciantini 09

PARTICLE ACCELERATION AT THE MOST RELATIVISTIC SHOCKS IN NATURE

RELATIVISTIC SHOCKS IN ASTROPHYSICS









PROPERTIES OF THE FLOW AND PARTICLE ACCELERATION

PARTICLE ACCELERATION AT THE HIGHLY RELATIVISTIC TERMINATION SHOCK

A COLLISIONLESS SHOCK: TRANSITION BETWEEN NON-RADIATIVE (UPSTREAM) AND RADIATIVE (DOWNSTREAM) TAKES PLACE ON SCALES TOO SMALL FOR COLLISIONS TO PLAY A ROLE

SELF-GENERATED ELECTROMAGNETIC TURBULENCE MEDIATES THE TRANSITION: IT MUST PROVIDE BOTH THE DISSIPATION AND PARTICLE ACCELERATION MECHANISMS

> THE DETAILED PHYSICS AND THE OUTCOME OF THE PROCESS STRONGLY DEPEND ON COMPOSITION ($e^{-}-e^{+}-p$?) MAGNETIZATION ($\sigma=B^{2}/4\pi n\Gamma mc^{2}$) GEOMETRY ($\Gamma \times \Theta(B \cdot n)$) OF THE FLOW

PARTICLE ACCELERATION MECHANISMS

COMPOSITION: MOSTLY PAIRS MAGNETIZATION: 5>0.001 FOR MOST OF THE FLOW GEOMETRY: TRANSVERSE

REQUIREMENTS:

✓OUTCOME: POWER-LAW WITH α~2.2 FOR OPTICAL/X-RAYS α~1.5 FOR RADIO
 ✓MAXIMUM ENERGY: FOR CRAB ≈FEW x 10¹⁵ eV (CLOSE TO THE AVAILABLE POTENTIAL DROP AT THE PSR)
 ✓EFFICIENCY: FOR CRAB ~20% OF TOTAL L_{sd}

PROPOSED MECHANISMS:

FERMI MECHANISM IF/WHERE MAGNETIZATION IS LOW ENOUGH
SHOCK DRIFT ACCELERATION
ACCELERATION ASSOCIATED WITH MAGNETIC RECONNECTION TAKING PLACE AT THE SHOCK (Lyubarsky & Liverts 08)
RESONANT CYCLOTRON ABSORPTION IN ION DOPED PLASMA (Hoshino Et Al 92, Amato & Arons 06)

PROS & CONS OF DSA AND SDA

-SDA NOT EFFECTIVE AT SUPERLUMINAL SHOCKS(!!) UNLESS UNREALISTICALLY HIGH TURBULENCE LEVEL (Sironi & Spitkovsky 09)

+IN WEIBEL MEDIATED (UNMAGNETIZED) e⁺-e⁻ SHOCKS FERMI ACCELERATION EFFECTIVE (Spitkovsky 08)

+POWER LAW INDEX OK FOR THE OPTICAL/X-RAY SPECTRUM OF CRAB (Kirk et al 00) BUT e.g. VELA SHOWS FLATTER SPECTRUM (Kargaltsev & Pavlov 09)

-SMALL FRACTION OF THE FLOW SATISFIES THE LOW MAGNETIZATION (σ <0.001) CONDITION (SEE MHD SIMULATIONS)

DRIVEN MAGNETIC RECONNECTION

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(Sironi & Spitkovsky 12)

RESONANT ABSORPTION OF ION CYCLOTRON WAVES



+++++

PULSAR MULTIPLICITY CANNOT BE LARGER THAN 10⁴

RESONANT CYCLOTRON ABSORPTION IN ION DOPED PLASMA



LEADING EDGE OF A TRANSVERSE RELATIVISTIC SHOCK IN 1D PIC



SUBILETIES OF THE RCA PROCESS



1D PIC sim. with m_i/m_e up to 20 (Hoshino & Arons 91, Hoshino et al. 92) Showed e⁺ effectively accelerated if U_i/U_{tot}>0.5

For low mass-ratios U_i/U_{tot}>0.5 requires large fraction of p That makes waves circularly polarized and preferentially absorbed by e⁺

> For m_i/m_e=100: polarization of waves closer to linear Comparable acceleration of both e⁺ and e⁻



SUBTLETIES OF THE RCA PROCESS II



EFFECTS OF THERMAL SPREAD



PARTICLE SPECTRA AND ACCELERATION EFFICIENCY



Acceleration efficiency: ~few% for U_i/U_{tot}~60% ~30% for U_i/U_{tot}~80%

Spectral slope: >3 for U_i/U_{tot}~60% <2 for U_i/U_{tot}~80%

$\begin{array}{l} \hline \textbf{ELECTRON ACCELERATION!!!}\\ LESS EFFICIENT THAN FOR POSITRONS:\\ (LOW m_i/m_e \Rightarrow LARGE n_i/n_e TO ENSURE U_i/U_{tot} > 0.5) \rightarrow ELLIPTICAL\\ POLARIZATION OF THE WAVES\\ \hline \textbf{EXTRAPOLATION TO REALISTIC m_i/m_e PREDICTS SAME EFFICIENCY}\\ RESULTS RECENTLY CONFIRMED BY Stockem et al 12\\ \hline \end{array}$

THINGS YOU GET FOR FREE

If Γ ~ few x 10⁶

✓NICELY FITS WITH CORRELATION (Gotthelf 03) BETWEEN X-RAY EMISSION OF PSRs AND PWNe: EVERYTHING DEPENDS ON u_i/u_{tot} AND ULTIMATELY ON ELECTRODYNAMICS OF UNDERLYING COMPACT OBJECT

✓MAXIMUM ENERGY ~ WHAT REQUIRED BY OBSERVATIONS

 \checkmark REQUIRED (dN_i/dt)~10³⁴ s⁻¹~(dN_i/dt)_{GJ} FOR CRAB: RETURN CURRENT FOR THE PULSAR CIRCUIT

✓NATURAL EXPLANATION FOR CRAB WISPS (Gallant & Arons 94)
 AND THEIR VARIABILITY (Spitkovsky & Arons 04)
 (ALTHOUGH ALSO DIFFERENT EXPLANATIONS WITHIN IDEAL
 MHD: TIME-SCALES TURN OUT TO BE THE SAME)

PUZZLE WITH K

IF MULTIPLICITY IS 10⁵-10⁶ IONS CANNOT DOMINATE THE ENERGY

REMINDER:LOSS-LIMITED ACCELERATION

$$t_{loss} = \frac{E}{\left(\frac{dE}{dt}\right)_{sync}} = \frac{6\pi}{\sigma_T} \frac{mc}{B^2 \gamma}$$

$$t_{acc} = \frac{E}{\left(\frac{dE}{dt}\right)_{acc}} \ge \frac{m\gamma c^2}{e\left|\vec{E}\right|c} = \frac{m\gamma c}{feB} \qquad f \le 1$$

$$t_{acc} = \eta \frac{D_B}{u^2} = \eta \frac{cr_L}{c^2} = \eta \frac{m\gamma c}{eB} \quad \eta \ge 1$$

$$t_{acc} \le t_{loss} \implies \gamma_{max} = \sqrt{f \frac{6\pi e}{B\sigma_T}} \approx 1.5 \times 10^{10} \frac{\sqrt{f}}{\sqrt{B[100\,\mu G]}}$$

$$\varepsilon_{\max} = \frac{3h}{2} \frac{eB}{2\pi mc} \gamma_{\max}^2 = f \frac{9h}{2} \frac{e^2}{mc\sigma_T} \approx 230 f MeV$$

WHAT IS f WITHIN RCA?

VARIABILITY WITHIN RCA

RCA Mechanism has an intrinsic maximum energy:

$$\omega_{c\pm} \ge \omega_{ci} \implies \frac{1}{m_{\pm}\gamma_{\pm}} \ge \frac{1}{m_{i}\gamma_{i}} \implies \gamma_{\max}^{RCA} = \frac{m_{i}}{m_{e}}\Gamma_{wind} \approx 6 \times 10^{9} \frac{\Gamma_{wind}}{3 \times 10^{6}}$$
Based on 1d PIC of RCA
(Amato & Arons 06)
f~.1-.5 (σ and E_{i}/E_{tot})
Caveat: in 3D?
$$\gamma_{\max}^{loss} = 1.2 \times 10^{10} \sqrt{\frac{f}{B_{-4}}} \approx 2.5 \times 10^{9} \sqrt{\frac{f_{1/2}}{B_{-3}}}$$
Fermi steady
cut-off
$$\varepsilon_{\max} \approx 100 f_{1/2} MeV \approx 100 \frac{B}{10^{-3}} \left(\frac{\gamma_{\max}}{2.5 \times 10^{9}}\right)^{2} MeV$$

$$I$$

$$T_{var} \approx 3 \left(\frac{\varepsilon_{ph}}{100 MeV}\right)^{1/2} \left(\frac{f}{0.5}\right)^{-1} \left(\frac{B}{mG}\right)^{-3/2} days$$
Type and ε_{\max} in the ballpark...
Special relativity could help: $\varepsilon_{\max}^{obs} \approx \Gamma \varepsilon_{\max}^{rf}$

$$T_{var}^{obs} \approx \Gamma^{-1} T_{var}^{rf}$$

SIGNATURES OF RELATIVISTIC PROTONS

If protons are there, they might reveal themselves through π -production (Bednarek 02; Amato et al 03)

$$\boxed{\pi^{0} \rightarrow \gamma \text{-rays}} \leftarrow \boxed{L_{\pi} = f_{\pi} L_{p}} \rightarrow \boxed{\pi^{\pm} \rightarrow e^{\pm} \nu}$$

Fluxes of all secondaries depend on U_i/U_{tot} , Γ and target density





DEPENDENCE ON CRAB WIND $L_p = L_B = L_{e^{\pm}} = (1/3)L_0$ PARAMETERS



THE POSITRON "EXCESS"

Ackerman et al 11



PULSARS AND THEIR WINDS



PULSARS ARE EXCELLENT ANTI-MATTER FACTORIES

PAIRS ARE ACCELERATED WITH

 $L_{\text{PAIRS}} \approx 20\text{-}30\% L_{\text{PSR}}$

N_{PAIRS}(E)∞E^{-γ} 1<γ<1.5 FOR E<.1-.5 TeV

(ALL FROM OBSERVATIONS!)

WHAT HAPPENS TO THE PAIRS?

THE PAIRS INSIDE THE PWN TRY TO EXPAND AGAINST THE EJECTA SUFFERING ADIABATIC+RADIATIVE LOSSES

WHEN THE REVERSE SHOCK OF THE BLAST WAVE REACHES THE CENTER, SOME LEVEL OF COMPRESSION MIGHT OCCUR

...BUT IT COULD EVEN DISPLACE THE PWN (SEE CASE OF VELA), POSSIBLY LIBERATING SOME ELECTRONS AND POSITRONS

IN GENERAL HOWEVER THE ELECTRONS AND POSITRONS STAY INSIDE THE REMNANT AND KEEP LOSING ENERGY BOTH RADIATIVELY AND ADIABATICALLY

BUT DO WE REALLY NEED TO RETRIEVE THESE PAIRS FROM IN THERE?

A HIGH VELOCITY POPULATION



PULSAR BOW SHOCK NEBULAE

MOUSE NEBULA





MAIN UNKNOWN: HOW MUCH ENERGY IS LEFT IN PAIRS AT THIS TIME?

DEPENDS ON SPIN-DOWN: $L = I\Omega\Omega \propto \Omega^{n+1}$ •n=3 FOR DIPOLE

OBSERVED VALUES: ALWAYS n<3

ENERGETICS

THE ENERGY AVAILABLE AFTER A TIME T_{*} WHEN THE NS IS OUTSIDE THE SNR IS

$$E_* = E(t > T_*) = \frac{1}{2} I \Omega_0^2 \left(1 + \frac{T_*}{\tau_0} \right)^{-\frac{2}{n-1}} = E_{tot} \left(1 + \frac{T_*}{\tau_0} \right)^{-\frac{2}{n-1}}$$

FOR T_{*}~40,000 YEARS, ONE HAS:

$$\frac{E_*}{E_{tot}} \approx 0.5 \quad \text{For dipole n} = 3$$
$$\frac{E_*}{E_{tot}} \approx 0.02 \quad \text{For n} = 2.5$$

WE WILL SEE LATER HOW THIS COMPARES WITH ENERGETIC REQUIREMENTS IMPOSED BY PAMELA RESULTS


PARTICLE SPECTRA FROM IN THE TWO CASE **FIGURE FILL FILL OF A FILL OF A CONTROL OF**



PSR J1509-5850 SLOPE RADIO: -0.26 SLOPE ELECTRONS: -1.52 Ng et al. 2010



THE MOUSE SLOPE RADIO: -0.3 SLOPE ELECTRONS: -1.6

ELECTRONS AND POSITRONS FROM PULSARS

e++e-

Blasi & Amato 11

TOTAL

SNRs

QuickTime[™] and a decompressor are needed to see this picture.

PWNe

25% EFFICIENCY FOR n=2.5

1% EFFICIENCY FOR n=3

CONTRIBUTION FROM PULSARS MUST BE THERE AT SOME LEVEL!!!!

SUMMARY

- +THE BEST WAY TO LEARN ABOUT PSR ELECTRODYNAMICS IS BY LOOKING A PWNe
- +2D AXISYMMETRIC MHD MODELS ARE VERY SUCCESSFUL AT REPRODUCING THE SPATIAL FEATURES OF THE EMISSION
- +THEY ALLOW US TO CONSTRAIN THE FLOW MAGNETIZATION AT TS
- +THEY CAN ALSO ACCOUNT FOR VARIABILITY IN THE INNER NEBULA ON WEEK-MONTH TIME-SCALES
- +PREDICTION OF MILDLY RELATIVISTIC FLOW IN THE DOWNSTREAM ALSO HELPS WITH ACCOUNTING FOR PUZZLING FERMI CUT-OFF

-WE DO NOT UNDERSTAND HOW PARTICLES ARE ACCELERATED AT THESE EXTREME SHOCKS

-WE DO NOT HAVE A GOOD EXPLANATION FOR FLARES YET

COSMIC RAY RELATED ISSUES: •PWNe ARE LIKELY TO BE THE PRIMARY CONTRIBUTOR TO THE CR POSITRON EXCESS •WE STILL DO NOT KNOW WHETHER THEY CONTAIN MULTI-PEV IONS